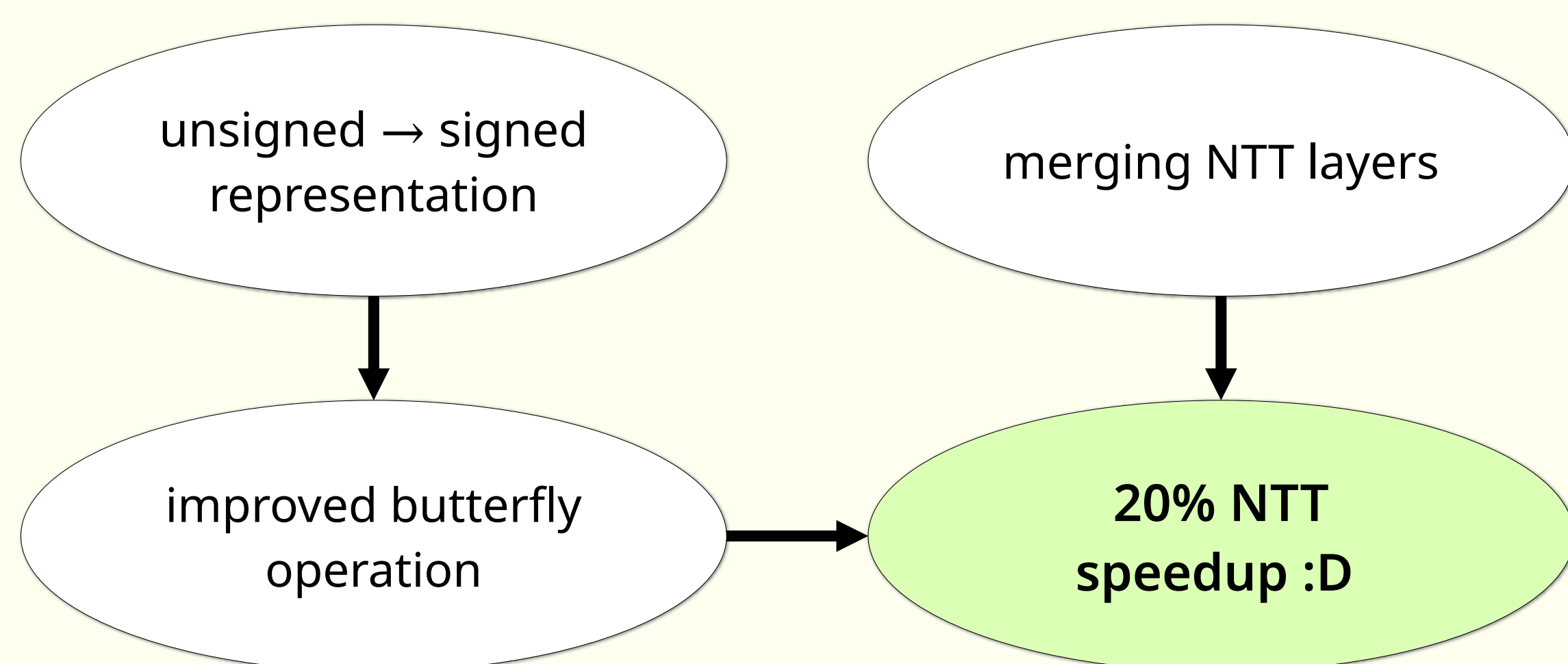


# Compact Dilithium Implementations on Cortex-M3 and Cortex-M4

<https://ia.cr/2020/1278>

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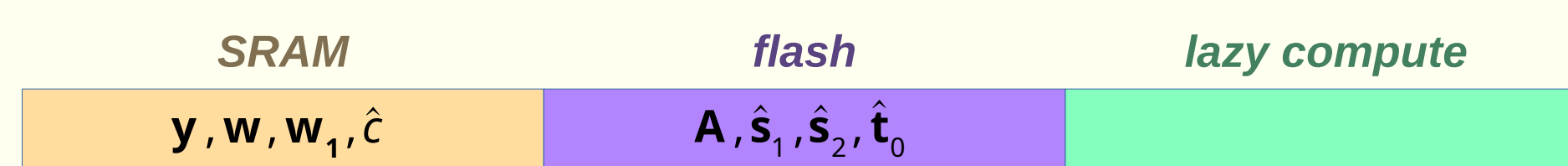
## Performance



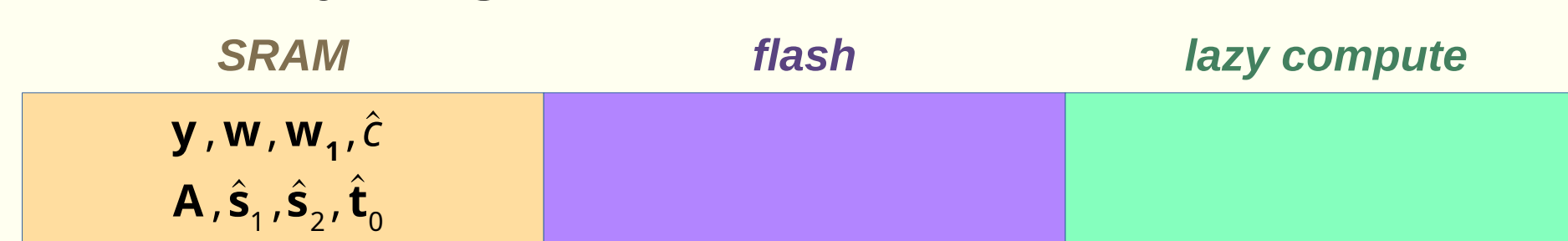
## Memory

Some Dilithium values need a lot of storage. We investigate how their storage location impacts the memory usage and speed.

**Method 1.** Store the public key in flash memory.



**Method 2.** Everything in SRAM.



**Method 3.** "Lazy" compute as much as possible.



## Results

Algorithm & method	Work	Cortex-M4		Cortex-M3	
		Speed [kcc]	Stack [B]	Speed [kcc]	Stack [B]
Keygen (1)	<i>This work</i>	3 545	15 916 <sup>ab</sup>	4 503	15 703
Keygen (2 & 3)	[GKOS18]	2 320	50 488	—	—
	<i>This work</i>	2 013	8 940	2 562	9 007
Sign (1)	[RGCB19, scen. 2]	5 495	—	—	—
	<i>This work</i>	4 578	17 628 <sup>b</sup>	8 730	18 083
Sign (2)	[GKOS18]	8 348	86 568	—	—
	[RGCB19, scen. 1]	7 085	—	—	—
Sign (3)	<i>This work</i>	6 053	52 756	10 667	53 959
	<i>This work</i>	23 550	9 948	33 229	10 495
Verify	[GKOS18]	2 342	54 800	—	—
	<i>This work</i>	1 917	10 028	1 917	10 028

<sup>a</sup> Updated value was incorrect in the original paper.

<sup>b</sup> Uses an additional 34 896 bytes of flash space.

### Platforms & benchmarking

- Dilithium version is NIST round-2
- Results describe security level "Dilithium3" (more in the paper)
- Cortex-M4 platform: STM32F407 Discovery board @ 24 MHz
- Cortex-M3 platform: Arduino Due (SAM3X8E) @ 16 MHz

### Takeaways

- 20% faster NTT on Cortex-M4
- 7% faster keygen
- 15% faster signing
- 9% faster verification
- New Cortex-M3 implementation :D

### Cortex-M3 challenges

- `smull` & `smlal` not constant time!
- have to use Schoolbook (SB) multiplication on Cortex-M3
- only needed for computing with *secrets*

**SBSMULL** 9 cycles

```

; Input: a = a0 + a1*2^16
;         b = b0 + b1*2^16
;         c = c0 + c1*2^32
; Output: c = c + a*b
;         = c0 + c1*2^32
mul tmp, a0, b0
adds c0, c0, tmp
mul tmp, a1, b1
adc c1, c1, tmp
mul tmp, a1, b0
mla tmp, a0, b1, tmp
adds c0, c0, tmp, lsl #16
adc c1, c1, tmp, asr #16
                    
```

**SBSMLAL** 7 cycles

```

; Input: a = a0 + a1*2^16
;         b = b0 + b1*2^16
; Output: c = a*b = c0 + c1*2^32
mul c0, a0, b0
mul c1, a1, b1
mul tmp, a1, b0
mla tmp, a0, b1, tmp
adds c0, c0, tmp, lsl #16
adc c1, c1, tmp, asr #16
                    
```

### Scheme comparison (updated to 2022)

Algorithm	Public key [B]	Signature [B]	Sign [kcc]	Verify [kcc]
Falcon-1024 [PQM4]	1 793	1 280	85 161	978
SPHINCS+ (shake256-192s-robust) [PQM4]	48	16 224	93 294 080	83 021
Dilithium3 [PQM4,AHKS22]	—	—	6 610	2 691
Dilithium3 [BRS22]	1 952	3 293	36 303	7 249

### Acknowledgements

- This work has been supported by the European Commission through the ERC Starting Grant 805031 (EPOQUE), <3
- @Bo-Yin Yang: Thank you for all your valuable comments and the Institute of Information Science at Academia Sinica in Taipei, Taiwan, for housing and supporting MJK during the COVID-19 pandemic. This paper would not have been written otherwise.
- @Peter Pessl: Thank you for pointing out various improvements to our stack optimizations.

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